Quantum Weirdness
Part 4

The Uncertainty Principle
Interpretations Of Quantum Mechanics
Quantum Tunnelling

Interpretations of Quantum Mechanics
What does it mean?

The Copenhagen Interpretation

• A wavefunction describes the quantum system completely, in a probabilistic manner
• Any act of observation of the system causes the wavefunction to collapse into a definite state
• There must be unanswerable questions as to the quantum state before the measurement

This contradicts the classical view of physics: that it is always possible to know everything, if you measure it precisely enough

Who Invented the Term?

• The name appears to have been invented by Werner Heisenberg in the 1950s, when alternative interpretations appeared

Correspondence Principle

• Quantum mechanics must produce the same results as classical physics, if there are enough particles.
• Bohr was first to originate this in 1913, in his hydrogen atom model
• Special relativity (particles moving fast) reduces to Newtonian physics when the particles move slowly
• General relativity reduces to Newtonian gravity, when dealing with weak gravitational systems
• Inheritance from chromosomes reduces to Mendelian inheritance in organisms
Pilot Wave Theory/Bohm Interpretation

- de Broglie
- Bohm

Sometimes called a "hidden variable" theorem – not a good name!

• The Pilot Wave model got a boost in 2006, when Couder and Fort noticed that bouncing droplets, could be "walked" along the wave that they generated

https://www.youtube.com/watch?v=nmC0ygr08tE&feature=youtu.be

Stationary Bouncing Particles Walking particles

• Very recent experiments (2015-2016) have cast doubt on this

The experiments were done by Tomas Bohr – the grandson of Nils Bohr

https://www.youtube.com/watch?v=5TypwAwmPew&feature=youtu.be


Many Worlds Interpretation

- Hugh Everett III (1930-1982)
- Popularized by Bryce Seligman Dewitt


Everett did not believe that the underpinnings of quantum mechanics lead naturally to the correspondence principle.
Which is the original Monty? Is there any such thing as “I”? Are the various Montys connected?

In our universe the particle must only go through one slit. BUT we can see the result of an alternate universe, where the particle goes through the other slit, because we observe the interference pattern.

Still No Agreement on Interpretation!

- We can use Schrodinger’s Equation to calculate many things, even if we don’t understand the interpretation
- The physicist David Mermin describes his attitude to the Copenhagen Interpretation as “Shut up, and calculate”

Special Relativity

When things move very fast

The Speed of Light

- Maxwell’s equations predict that the speed of light in a vacuum is $c = 3.00 \times 10^8$ m/s
- This was confirmed in many experiments
- Most waves seen at this time (1880s) were mechanical waves. They needed a propagation medium
- e.g. sound needs air to propagate through
- Physicists assumed that EM waves must have some propagation medium – the luminiferous ether

The Ether Wind

- The earth was not expected to be stationary in the ether
- The speed of light measured on earth should vary depending on the relative speed of the earth with respect to the ether
- Headwinds and Tailwinds
The Michelson-Morley Experiment

- Albert Michelson and Edward Morley
- Measured the speed of light using a 35 km long interferometer at various points in the year (different places on the orbital path of the earth)
- A NULL RESULT
- No difference in the speed of light at any time of the year
- NO LUMINIFEROUS ETHER

Einstein’s Special Theory of Relativity (1905)

- The laws of physics must be the same for all non-accelerating observers
- The speed of light in a vacuum has the same value regardless of the velocity of the observer and the velocity of the source
- There is no unique inertial frame (everything is relative!)

At high speeds, near to the speed of light, the familiar equations in classical mechanics need to be modified by an extra factor $\gamma$

- The Lorentz factor $\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$

Momentum = $mv$ (Newton)
Momentum = $\gamma mv$ (Relativistic)

Hendrik Antoon Lorentz
Nobel Prize 1902

When an object moves very quickly, time appears to move at a different rate according to an outside observer

- A clock travelling with the moving object does not change speed

To the stationary observer, the moving clock has moved more quickly. Less time elapses for the moving clock than the stationary clock

The Twin Paradox

Scott Kelly (left) and his twin brother Mark Kelly (right). Both astronauts

Scott spent a year on the International Space Station, moving at 27,000 km/h with respect to the Earth. His body clock slowed down very slightly compared to his twin Mark

Mark aged slightly more than Scott (a few microseconds per day)

Quantum Mechanics and Special Relativity

Quantum Particles Moving Very Quickly
P.A.M. Dirac

- Paul Adrien Maurice Dirac
- British mathematician, physicist and engineer
- Combined the Schrödinger Equation with Special Relativity to deal with quantum systems with particles moving at high speeds.

The Dirac Equation

\((i\hbar \partial - m)\psi = 0\)

- Dirac used matrices to modify Schrödinger’s Equation to handle Special Relativity
- He noticed that it was possible to get negative energy solutions from the equation.
- This was the first prediction of anti-matter

Antimatter

- Solutions to the Dirac Equation predicted that for every particle of matter, there must be an antiparticle (antimatter).
- The antimatter counterpart of the electron is the positron
- It has exactly the same mass as the electron, but has a positive charge instead of negative

Matter-Antimatter Annihilation

- If a matter particle meets the antimatter counterpart they annihilate each other
- For the electron-positron reaction, the matter disappears and is replaced by two gamma ray photons. (This conserves momentum and energy)
- A free positron never has to go far in order to meet an electron.

- When the positron and the electron annihilate each other, energy and momentum must still be conserved
- A pair of gamma ray photons, moving in opposite directions are produced

- We use this pair production to localize the site of cancer tumour
- Tumours have a fast metabolism, so take up sugars faster than normal tissue
- Fluorodeoxyglucose (\(^{18}\text{F}\)) is a glucose analogue with a radioactive fluorine-18 substituted instead of an –OH
• It concentrates at the site of the tumour

• It decays with a half-life of 110 minutes into oxygen, a positron and a neutrino

\[ ^{18}_9F \rightarrow ^{18}_8O + e^+ + \nu \]

Beta+ decay:
Proton becomes a neutron, a positron and a neutrino

• More positrons are produced in the tumour than in the surrounding normal tissue
• They annihilate with electrons giving off gamma rays
• More gamma rays produced at the tumour than elsewhere

Positron Emission Tomography

• An imaging technique using the production of the gamma rays to determine the site of the emission

Dr Heather Williams (Medical Physicist at the Christie Hospital in Manchester)

Normal Brain scan: false colour image

Pair Production – Mass From Energy

• Pair Production, the reverse process to pair annihilation is possible
• A highly energetic photon, passing close to a nucleus can transform itself into a pair of particles, an electron and a positron
• Mass is created during this process, since the photon has no mass
Charged particles follow a spiral path in a magnetic field. Opposite charges spiral in opposite directions.

Quantum Electrodynamics (QED)
- Dirac extended Maxwell’s Electromagnetism Formulations to allow for collections of quantum particles.
- This could account for the annihilation processes
- Requires the virtual particles allowed by the Uncertainty Principle

- [https://www.youtube.com/watch?v=crfY2vVMbl](https://www.youtube.com/watch?v=crfY2vVMbl)

Quantum Tunnelling
- How to get out of a box by quantum cheating
- In classical physics, a particle trapped inside a potential well (the particle in the box) can never get out, unless extra energy is supplied, so it can “climb over” the wall.
- Quantum physics allows us to cheat!
- Minute Physics
- [https://www.youtube.com/watch?v=cTodS8hkSDg](https://www.youtube.com/watch?v=cTodS8hkSDg)

- Physicist talk about objects in “Potential Wells”
- Objects trapped in the well caused by the gravitational field of the earth
- In classical physics, the only way to get out of the well, is to have some supply of external energy
  - Haul the dog out with a crane
  - OR
  - dog jumps out if it uses energy reserves in muscles

- [https://www.youtube.com/watch?v=cTodS8hkSDg&feature=youtu.be](https://www.youtube.com/watch?v=cTodS8hkSDg&feature=youtu.be)
Potential Wells in Atoms

Electrical Potential Wells

- Coulomb Forces between charged particles
  - Like charges repel
  - Unlike charges attract

\[ F \]

In atoms and molecules, negative electrons move around a positive nucleus

- The electrons are in the potential well generated by the proton

The Hamiltonian Operator in the Schrodinger Equation defines the shape of the potential well

- The simplest shape of well, is one with infinitely high walls, and a flat bottom

\[ F(x) = \infty \quad \text{(barrier)} \]
\[ F(x) = 0 \quad \text{(well)} \]
\[ F(x) = \infty \quad \text{(barrier)} \]

- This is not a very realistic model
- The solutions to the Schrodinger equation are mathematically simple!

In an infinitely deep well, the quantum particle cannot get out

- The solutions to the Schrodinger Equation are standing waves
- Just like the waves on a string

More realistic potential well. Particles in the well can escape

In classical physics – they need extra energy from outside

\[ F(x) = 0 \quad \text{(well)} \]

Finite Height

Finite Width
In quantum physics the solutions to the Schrödinger equation predict a probability outside the well. High Probability that the wave stays inside the well, Low probability that wave is outside the well.

Applications of Quantum Tunnelling
How we can use this.

Scanning Tunnelling Microscope
- Directly observing positions of atoms, by looking at the electron clouds around them.

Tungsten tip – so sharp that it ends in one atom.
Electron tunnels from tip to the surface.

Tunnelling probability is very sensitive to the distance between the tip and the surface:
\[ a = 1.000 \text{ nm} = 1.000 \times 10^{-9} \text{m} \]

Tunnelling increases as the tip passes over places with a high probability of an electron.
Scanning Tunnelling Microscope head

Tip (platinum-iridium alloy)

Nanoscale Manipulation

- The STM tip can be used to move individual atoms around the surface and position them precisely

US National Institute of Standards and Technology

A 40-nanometre-wide NIST logo made with cobalt atoms on a copper surface.

Quantum Corral

Iron atoms

Quantum Well

Ripples are the wavefunction of an electron trapped in the corral

Quantum Dot: Switching By Tunnelling

Electron energy

Energy levels in quantum dot

Voltage (V)

0.0  0.5  1.0  1.5  2.0  2.5  3.0  3.5  4.0  4.5  5.0